

An Introduction to Rasch Analysis

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Outlines

- Introduction
- Rasch Analysis Categories
- Rasch Analysis in R

Learning outcomes

- Understand the basic concepts in Rasch analysis
- Perform Rasch analysis for dichotomous items

Introduction

What is Rasch Model

- George Rasch's Measurement Model in 1960
- A probabilistic model for intelligence and attainment tests
- Probability of correct answer depends on TWO facets: Person Ability and Item Difficulty (Facility)

What is Rasch Model

- $P(\text{Correct}) \leftarrow \text{Person Ability} + \text{Item Difficulty}$
(Facility)
- $\uparrow \text{Ability} + \downarrow \text{Difficulty} \rightarrow \uparrow \text{Pr}(\text{Correct})$
- $\downarrow \text{Ability} + \uparrow \text{Difficulty} \rightarrow \downarrow \text{Pr}(\text{Correct})$

What is Rasch Model

- Map Ability and Difficulty on the same standardized scale using Logit Transformation
- Proportion (p) of correct \rightarrow Log Odds

$$\text{Odds} = \frac{p}{(1 - p)}$$
$$\log \text{Odds} = \log(\text{Odds})$$

What is Rasch Model

- Ability of Person i is

$$B_i = \log \left[\frac{p_i}{1 - p_i} \right]$$

- Difficulty of Item j is

$$D_j = \log \left[\frac{p_j}{1 - p_j} \right]$$

What is Rasch Model

- Probability of correct (X) for Person i and Item j based on Rasch model is

$$P(X_{ij}=1 | B_i, D_j) = \frac{\exp(B_i - D_j)}{1 + \exp(B_i - D_j)}$$

Practical

- Let's calculate all these in Excel
- data_10.xls > Ability & Difficulty (original data from Dr. Nurhanis)

Rasch Analysis Categories

Analysis Categories

Three categories of Rasch analysis:

- Calibration
- Model-data fit
- Other validity evidence

Calibration

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Fit Rasch model to estimate:

- Each Item **Difficulty**
- Each Person **Ability**

Range:

-ve → zero → +ve
Easier → Middle → Difficult
Weak → Middle → Bright

NO Discrimination – not part of Rasch model, assumed to be the same and constant (= 1)

Model-data fit

Three categories of Rasch analysis activities:

- Calibration
- Model-data fit
- Other validity evidence

Before calibration:

Dimensionality assessment –
unidimensionality (one dimension / trait)

- Factor analysis for categorical data
- EFA on tetrachoric correlations
- CFA using estimation methods that handle categorical data

After calibration:

Item & Person Fits

- INFIT – weighted fit statistics
- OUTFIT – unweighted fit statistics
- SEPARATION RELIABILITY – like Cronbach's alpha

Unidimensionality

Graphical assessment

Model-data fit

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Around 1 for raw /
Around 0 for z/t (± 2)

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Around 1 for raw /
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Responses **NEAR** an item's difficulty
closely match what are expected by
the model

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Same as alpha > 0.7
Consistency

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Model-data fit

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How well an instrument can separate items in terms of their latent variable difficulties

Same as alpha > 0.7
Consistency

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- % variance explained
- PCA of standardized residuals

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- Maps – Wright's & Pathway
- Item characteristic curve (ICC)

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Other validity evidence

Three categories of Rasch analysis activities:

- Calibration
- Model-data fit
- Other validity evidence
 - Invariance of item parameters
 - Differential item functioning (DIF)
 - Other typical construct validity evidence

Other validity evidence

Three categories of Rasch analysis activities:

- Calibration
- Model-data fit
- Other validity evidence
 - Split sample into two-halves randomly
 - Fit Rasch model
 - Correlate between two sample estimates
- Invariance of item parameters
- Differential item functioning (DIF)
- Other typical construct validity evidence

Other validity evidence

Three categories of Rasch analysis activities:

- Calibration
- Model-data fit
- Other validity evidence
 - Whether performance on any of the items differs for certain groups (e.g. male vs female)
 - Probability of correctly responding to an item should be the same for males and females
- Invariance of item parameters
- Differential item functioning (DIF)
- Other typical construct validity evidence

Other validity evidence

Three categories of Rasch analysis activities:

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- Other validity evidence

Comparison vs known criteria, other instruments/variables

- Invariance of item parameters
- Differential item functioning (DIF)
- Other typical construct validity evidence

Rasch Analysis in R

Practical

- Let's obtain all these in R
- `data_10.xls` (original data from Dr. Nurhanis)
- `practical_rasch.html` (tutorial in R)

References

- Bond, T. G., Yan, Z., & Heene, M. (2021). *Applying the Rasch model: Fundamental measurement in the human sciences* (4th ed.). Rouledge.
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- Wind, S., & Hua, C. (2022). *Rasch measurement theory analysis in R*. CRC Press.